



RECURSIVE FUNCTIONS

Introduction

- **Recursion** is a process by which a **function calls itself repeatedly**, until some specified condition has been satisfied.
- The process is used for **repetitive computations** in which each action is stated in terms of a previous result.

Introduction

- In order to solve a problem **recursively**, two conditions must be satisfied.
- **First**, the problem must be written in a recursive form, and **second**, the problem statement must include a stopping condition.

Recursion - Example

- Suppose, for example, we wish to **calculate the factorial of a positive integer quantity.**
- We would normally express this problem as:

$$n! = 1 \times 2 \times 3 \times \dots \times n$$

- where **n** is the **specified positive integer.**

Recursion - Example

- However, we can also express this problem in another way by

writing:

$$n! = n \times (n - 1)!$$

- This is a **recursive statement of the problem**, in which the desired action (**the calculation of n!**) is expressed in terms of a previous result [**the value of (n-1)!**, which is assumed to be **known**].

Recursion - Example

- Also, we know that $1! = 1$, by definition.
- *This last expression provides a stopping condition for the recursion.*



Calculating Factorials - Example

```
# include <stdio.h>

long int factorial ( int n ) {
int i;
long int prod = 1;
if ( n > 1)
    for ( i = 2; i<=n ; ++i)
        prod *= i;
    return(prod); }

void main ( void ) {
printf ( "\n 5! = %ld", factorial(5));
}
```

```
# include <stdio.h>

long int factorial ( int n ) {
if ( n <= 1)
    return 1;
else
    return ( n * factorial ( n - 1 ));
}

void main ( void )
{
printf ( "\n 5! = %ld", factorial(5));
}
```

Practice Questions

- Convert the following function into recursive function:

```
int sum(int n)
{
    int i, s = 0;
    for(i=1;i<=n;i++)
        s += i;
    return s;
}
```


Practice Questions

- Write a C function for the following mathematical formulations:

$$- F(x) = \begin{cases} n \cdot (n - 2), & n \text{ is positive and even} \\ n \cdot (n - 1), & n \text{ is positive and odd} \\ 1, & n < 0 \end{cases}$$

- Write a function to print the n^{th} term of Fibonacci series.
- Write a void returning recursive function to convert the given decimal no. system integer into its corresponding binary integer.